

The Influence of Needle Eccentric Motion on Hole-to-hole Injection Characteristics of a Two-layered 8-hole Diesel Injector

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Abstract

The stringent emission regulations diesel engines are required to meet has resulted in the usage of multi-hole and ultra-multi-hole injectors, nowadays. In this research study, a double layered 8-hole diesel injection nozzle was investigated both numerically and experimentally. A three-dimensional model of the nozzle which was validated with experimental results was used to analyze the injection characteristics of each hole. The validation was conducted by comparing experiment and simulation

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34 injection rate results, acquired simultaneously from all the holes of the injector and the model. The
35 fuel flow rates of the lower layered holes are higher than those of the upper layered holes. Two
36 different needle eccentricity models were established. The first model only included the lateral
37 displacement of the needle during needle lift. The needle reached maximum displacement at full
38 needle lift. The second model considered the needle inelastic deformation into consideration. The
39 needle radially displaces and glides along with the needle seat surface during needle lift. When the
40 eccentricity reached maximum in the radial direction, the needle began to lift upwards vertically.
41 The differences in injection characteristics under the different eccentricity models were apparent.
42 The results indicated that the cycle injection quantity, fuel injection rate and cavitation of each hole
43 were affected during the initial lifting stages of the needle lift. As the eccentricity of the needle
44 increases, the injection rate uniformity from the nozzle hole deteriorates. The result showed that the
45 upper layered holes were affected by the needle eccentricity during needle lift.

46 Key word: Diesel engine; Multi-hole injector; Injection rate; Needle eccentric movement

47 **1 Introduction**

48 The global awareness of environmental protection has resulted in the urgent need for pollutants
49 emission reduction through efficient combustion in Internal Combustion Engine (ICE). Therefore,
50 the continual improvement of engine combustion process through the optimization of injection
51 processes (in terms of fuel injection rates and spray characteristics) are considered as one of the
52 crucial methods of achieving substantial emission reduction during operation[1-3]. The fuel
53 injection rate affects the development of fuel spray directly and the interaction with the air in the
54 cylinder, influencing the combustion performance in the engine[4-5].

55 The needle is a key component in the nozzle and its reciprocating motion in the nozzle affects

56 the injection characteristics directly[6,8]. The needle motion is not always vertical due to the gap
57 between the needle and the needle guide. Needle guide length is limited and is not concentric with
58 the needle valve seat. The needle experienced elastic deformation under high pressure and develops
59 a cantilever effect when lifted[9,10]. This causes eccentricity in the radial directions, resulting in
60 flow and injection characteristics differences among the holes, which will affect the fuel injection
61 quality and atomization[11]. The more uneven the uniformity of the fuel distribution are, the worse
62 the uniformity of air-fuel mixture in the combustion chamber would be, resulting in the decline of
63 combustion quality, which ultimately affects the overall performance of the engine[12-18].

64 Present scholars mainly focus on the axial compression deformation of the needle and the effect
65 of needle lift on injection characteristics[19,20]. To determine the actual motion of the needle during
66 the opening and closing stages, researchers used various state of the art techniques to observe and
67 measure needle lift. Moon et al.[21] used X-ray phase contrast imaging (XPCI) to analyze the
68 transient needle movement of single-hole and multi-hole injectors. They found that the opening
69 speed of the needle rapidly increased and then decreased during the opening period of the needle
70 lift. When the number of holes increases, the maximum speed of opening the needle valve also
71 decreases. Kastengren et al.[22]used X-ray phase contrast imaging technology to observe the needle
72 movements of single-hole injector and three-hole injector. The maximum lifts of both injectors were
73 linear to their rail pressures. To determine why the needle behaves unconditionally during the needle
74 lift, the factors that influences the needle motion were also studied. Huang et al.[23]measured the
75 needle motion and near-field hydrodynamic characteristics inside the nozzle. Their results show that
76 needle lift is affected by the injection pressure during the opening stage. There is no obvious effect
77 by extending the injection pulse width at the same injection pressure. Furthermore, the effect of

78 needle movement on flow, injection and spray characteristics were studied extensively. Salvador et
79 al.[24]simulated the effects of different needle lifts on the flow characteristics inside the orifice
80 under steady state conditions. The nozzle flow coefficient reaches the maximum value at the quarter
81 of the maximum needle lift. The higher needle lift has no great effect on the flow coefficient and
82 fuel flow rate. Viera et al.[25]studied the relationship between the transient needle lift and the
83 corresponding injection rate. The results show that they are not linear and are affected by the
84 injection pressure; the needle lift speed also influences the fuel injection rate. Arienti et al.[26]
85 simulated the spray characteristics of n-dodecane with the needle movement under adiabatic and
86 isothermal wall conditions. As the needle gradually lifts, the gas is discharged as an incomplete jet.
87 The calculated injection rate is smaller than those measured in the experiment due to the
88 compressibility of the fuel.

89 The needle is one of the precision parts in the high-pressure common rail fuel injection system.
90 The guide gap of the upstream needle is usually only 1-2 μm to ensure the cooperation between the
91 needle and the needle body. X-ray phase contrast imaging and other test methods have determined
92 that the eccentricity of the downstream needle head of different injectors ranges up to 70 μm [27].
93 To observe the needle displacement from different nozzles, researchers have employed various
94 methods. Ohnishi et al.[28] drilled the head of the fuel injector. They observed the movement of the
95 needle head in the radial direction with a high-speed camera during the fuel injection process. The
96 results show that, for the Valve Covered Orifice (VCO) nozzle, the radial displacement of the needle
97 radia reached 65 μm . The needle of the MicroSac (MS) nozzle has a radial displacement for 24 μm .
98 Zhang et al.[29] used X-ray phase contrast imaging technology to observe and study the eccentric
99 motion of injectors with different nozzle structures to analyze the influence of injection parameters,

100 injection pressure and internal structure of the nozzle on the needle vibration. The results indicate
101 that the axial vibration amplitude of the needle is small while the radial oscillation amplitude is from
102 7 μm to 14 μm , which increases with the number of injection holes. The effects of the needle
103 displacement on fuel flow and injection characteristics were mostly investigated by means of
104 simulation (computational methods) by various researchers. Battistoni et al.[30] used the needle
105 eccentricity measured in the Argonne laboratory as the boundary condition to simulate the effect of
106 the three-dimensional movement of the needle on the transient fuel flow in the porous injector. The
107 results show that it affects the flow of fuel in the sac, resulting in the change of the parameters such
108 as the mass flow rate at the outlet of the hole, which will affect the atomization process. Wang et
109 al.[9] simulated the effect of needle eccentricity on the injection of the 6-hole VCO nozzle. The
110 uniformity of the injection of each nozzle hole becomes worse as the needle valve eccentricity
111 increases. Studies have shown that cavitation formation and spray characteristics developments are
112 influenced to some extent by the needle eccentric movement. Powell et al.[31] used X-ray
113 tomography and X-ray phase contrast imaging to observe the movement of the needle and the spray
114 development at the nozzle outlet. With this technique, they observed that the fuel flow in the sac is
115 significantly affected by the eccentric movement of the needle. Kim et al.[32] studied the effects of
116 different needle positions on spray and internal flow characteristics in a single-hole transparent
117 nozzle. They report that the spray cone angle and cavitation development are asymmetric as the
118 needle position deviates. Two different directions of the two stages off-axis needle displacement
119 were analyzed by Moro et al.[10]. Off-axis needle displacements in the immediate areas of the
120 nozzle orifices, causes exponential increment in spray jet penetrations as compared to off-axis
121 needle displacement around the maximum needle lift position.

122 Since the real nozzle hole is extremely small and the flow velocity in the nozzle hole is high,
123 the effect of eccentric motion by the needle on the injection rate is hard to measure through
124 experiments due to high cost and complexities[33,34]. Hence, Computational Fluid Dynamics (CFD)
125 simulation has been used in the research of injector spray characteristics widely. A three-dimensional
126 (3-D) model of the nozzle was used to analyze the injection characteristics of the nozzle after
127 validating with the experimental results. The validation was conducted by comparing experiment
128 and simulation injection rate results, acquired simultaneously from all the holes of the injector (with
129 a customized spray momentum flux experimental test rig[35-37]) and the model. VCO nozzles
130 exhibits higher flow sensitivities with regard to needle dynamics because of the direct relationship
131 that exist between the needle and the orifices. The changes in flow characteristic caused by needle
132 movement are directly propagated into the orifices. For the other nozzle types including blind hole
133 nozzle “SAC” and mini blind hole nozzle “MicroSac”, flow characteristic changes caused by needle
134 movement, are dampened by the sac volume to a little extent. The sac region, therefore, acts as a
135 buffering zone between the needle and the orifices[10]. The holes on the upper and lower layers of
136 a double-layer 8-hole sac injectors are evenly arranged circumferentially to expand the spatial
137 distribution of the fuel and arranged as many nozzles as possible under the sac volume size. When
138 the needle starts to move eccentrically, it will affect the fuel flow in the sac, hence influencing the
139 fuel injection quantity of the holes. Two types of needle eccentricities were established with
140 acceptable and reliable models. The first model considers the needle's lateral displacement during
141 needle lift. At maximum needle lift, the needle reached its largest displacement during the eccentric
142 movement. The second model took the needle inelastic deformation into consideration. The needle
143 displaces radially and rise along (glides) the needle seat surface without recovering. When the

144 maximum eccentricity in the radial direction is reached, the needle starts to rise vertically upward
 145 from the displaced position. Furthermore, the effects of different needle eccentric motions and
 146 eccentric parameters on the fuel injection rate of each hole, the cycle fuel injection quantity and the
 147 internal flow characteristics of the injection hole were analyzed in this study.

148 **2 Mathematical model**

149 **2.1 Calculation model**

150 Currently, homogeneous flow model, volume-of-fluid (VOF) model and two-fluid model are
 151 used to numerically study flow characteristics within nozzle hole. The two-fluid modeling approach
 152 were used to simulate the internal flow characteristics of a diesel injection nozzle in this study, since
 153 it provides the needed details with regards to flow distribution within the nozzle. This approach has
 154 been widely used in numerous research fields as it is generally considered to adequately replicate
 155 flow dynamics effectively. Using AVL Fire Eulerian-Eulerian multiphase module, the mass
 156 conservation and momentum conservation equations of the gas and the liquid phases are:

$$157 \quad \frac{\partial \alpha_k \rho_k}{\partial t} + \nabla \cdot \alpha_k \rho_k v_k = \sum_{l=1, l \neq k}^2 \Gamma_{kl} \quad (1)$$

$$158 \quad \frac{\partial \alpha_k \rho_k v_k}{\partial t} + \nabla \cdot \alpha_k \rho_k v_k v_k = -\alpha_k \nabla p + \nabla \cdot \alpha_k (\tau_k + T_k^l) + \alpha_k \rho_k g$$

$$159 \quad + \sum_{l=1, l \neq k}^2 M_{kl} + v_k \sum_{l=1, l \neq k}^2 \Gamma_{kl} \quad (2)$$

160 However, the volume fraction expression (Eq. 3) has to be satisfied

$$161 \quad \sum_{k=1}^2 \alpha_k = 1 \quad (3)$$

162 where α_k is the volume fraction of phase k , ρ_k is phase k density, v_k is phase k velocity, Γ_{kl} is
 163 the interfacial mass exchange between phases k and l , T_k^l is phase k Reynolds stress, and M_{kl} is
 164 the momentum interfacial interaction between phases k and l . For gas phase only, $k=1$ and for liquid
 165 phase only, $k=2$.

166 The 4-equationsk-zeta-f turbulent model was adopted for the replication of turbulence
 167 phenomenon within the two phase flow computations[38,39].

168 The basic expressions of the model are the turbulent kinetic:

$$169 \frac{\partial \alpha_k \rho_k k_k}{\partial t} + \nabla \cdot \alpha_k \rho_k \mathbf{v}_k k_k = \nabla \cdot \alpha_k \left(\mu_k + \frac{\mu_k^k}{\sigma_k} \right) \nabla k_k + \alpha_k P_k + \alpha_k P_{B,k} - \alpha_k \rho_k \varepsilon_k + \sum_{l=1, l \neq k}^2 K_{kl} + k_k \sum_{l=1, l \neq k}^2 \Gamma_{kl}$$

170 (4)

171 The turbulent dissipation:

$$172 \frac{\partial \alpha_k \rho_k \varepsilon_k}{\partial t} + \nabla \cdot \alpha_k \rho_k \mathbf{v}_k \varepsilon_k = \nabla \cdot \alpha_k \left(\mu_k + \frac{\mu_k^k}{\sigma_k} \right) \nabla \varepsilon_k + \sum_{l=1, l \neq k}^2 D_{kl} + \varepsilon_k \sum_{l=1, l \neq k}^2 \Gamma_{kl} + \alpha_k C_1 P_k \frac{\varepsilon_k}{k_k} -$$

$$173 \alpha_k C_2 \rho_k \frac{\varepsilon_k^2}{k_k} + \alpha_k C_3 \max(P_{B,k}, 0) \frac{\varepsilon_k}{k_k} - \alpha_k C_4 \rho_k \varepsilon_k \nabla \cdot \mathbf{v}_k \quad (5)$$

174 The velocity scale:

$$175 \frac{\partial \alpha_k \rho_k \zeta_k}{\partial t} + \nabla \cdot \alpha_k \rho_k \mathbf{v}_k \zeta_k = \nabla \cdot \alpha_k \left(\mu_k + \frac{\mu_k^k}{\sigma_k} \right) \nabla \zeta_k + \zeta_k \sum_{l=1, l \neq k}^2 \Gamma_{kl} - \alpha_k P_k \frac{\zeta_k}{k_k} + \alpha_k f_k \quad (6)$$

176 The elliptical function:

$$177 f_k = L_k^2 \nabla^2 f_k - \frac{1}{T_k} \left(C_1 - 1 + C_2 \frac{P_k}{\varepsilon_k} \right) \left(\zeta_k - \frac{2}{3} \right) \quad (7)$$

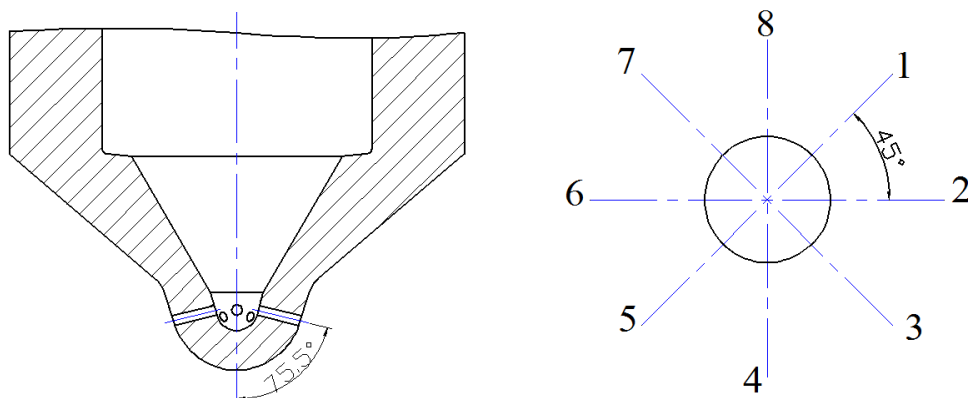
178 where, k_k is the turbulence kinetic energy at phase k , ε_k is the diffusivity of the turbulence kinetic
 179 energy at phase k , ζ_k is the velocity scales ratio at phase k , f_k is the elliptical function at phase k , P_k
 180 is the production term of the turbulence kinetic energy due to shear and $P_{B,k}$ is the generation
 181 component of the turbulence kinetic energy caused by buoyancy. The Prandtl number for the
 182 turbulence kinetic energy is σ_k , K_{kl} is the component of transmission between phases k and l , σ_ε
 183 is the Prandtl number for the ε equation and C_1, C_2, C_3, C_4 are constants. D_{kl} is the interfacial
 184 exchange component of the dissipation (ε) equation.

185 2.2 Computational meshing

186 The geometries of the eight holes diesel injector that is analyzed in this research is shown in

187 Fig. 1. The injector has a nozzle hole diameter of 0.18 mm, hole length of 0.65 mm ($l_1=l_2$). As seen
188 in Fig. 1, the nozzle holes (numbered from 1 to 8 in a clockwise order) are evenly distributed
189 circumferentially (i.e. 45° between adjacent nozzle holes). Also, all the nozzle holes make an
190 inclination angle of 75.5° as seen in the figure. The lower layered holes were 1, 3, 5 and 7 and the
191 upper layered were hole 2, 4, 6 and 8. The distance between the upper layer and the lower layered
192 was 0.12 mm.

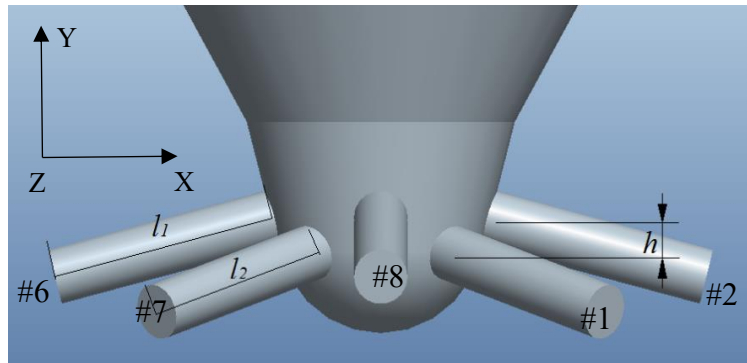
193 From the nozzle geometry (shown in Fig. 1), a three dimensional (3D) model of the nozzle was
194 developed with Pro Engineering (ProE) software as shown in Fig. 2. After a professional mesh
195 software (Hypermesh) was used to discretize the 3D model into structured hexahedral grid shown
196 in Fig. 3. The model was discretized into around 320,000 cells, as this quantity ensures the
197 independence of the simulation results. As seen in Fig. 3, areas within and around the nozzle holes
198 were meshed relatively smaller than the other areas. It is to ensure that the complex internal flow
199 characteristic of the nozzle holes is adequately captured and analyzed. The dynamics of the needle
200 during injection (needle movement) were simulated with moving mesh technique. With the moving
201 mesh, transient flow characteristics with regards to needle displacement within the nozzle were
202 obtained.



204 Fig. 1 Sectional views of the injection nozzle, showing the inclination angle of the nozzle hole on the left hand side

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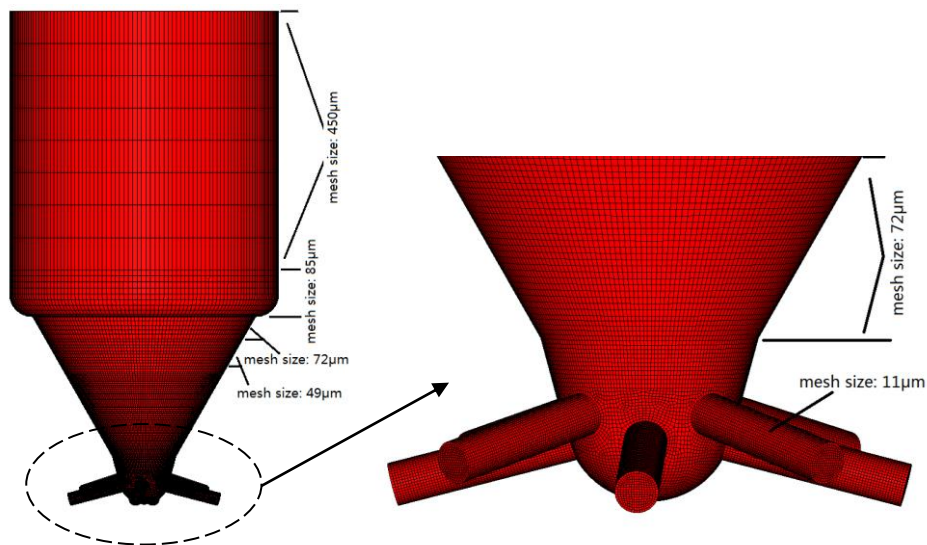
and the angle between the nozzle holes on the right hand side



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207

Fig.2 Sectional views of injection nozzle



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Fig. 3 The diagram of the computational grid

210

Since the total cell numbers of the model can influence the accuracy of the results and the

211

computational time, it was necessary to carry out mesh sensitivity analysis firstly before conducting

212

any investigation with the model. To ensure that the simulation results are independent of the mesh,

213

different mesh sizes of the model were generated and then simulated. As shown in Fig. 4, the average

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mass flow rate obtained from the various simulations were plotted against the total mesh numbers.

215

It can be seen from the figure that the mass flow rate begins to converge with regards to the cell

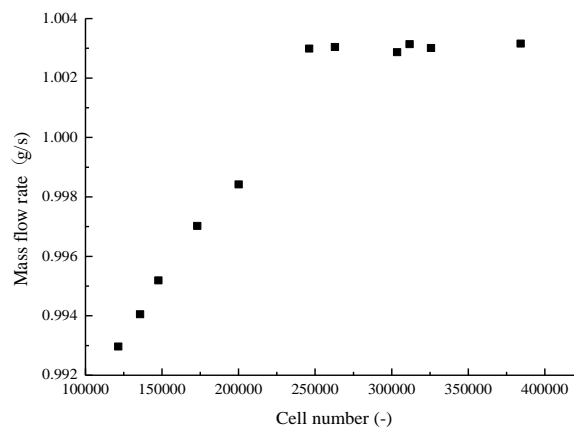
216

numbers when cell number reached approximately 250,000. From the cell numbers of 250,000

217

onwards, the mass flow rate is independent of the nozzle cell number. Hence, as earlier stated, the

218 model was discretized into around 320,000 cells totally in this investigation. The whole nozzle was
219 modelled because it provides more flow information than a symmetric section. Even though the
220 nozzle is a symmetric one, there will still be flow differences within the holes due to certain dynamic
221 factors within the nozzle.



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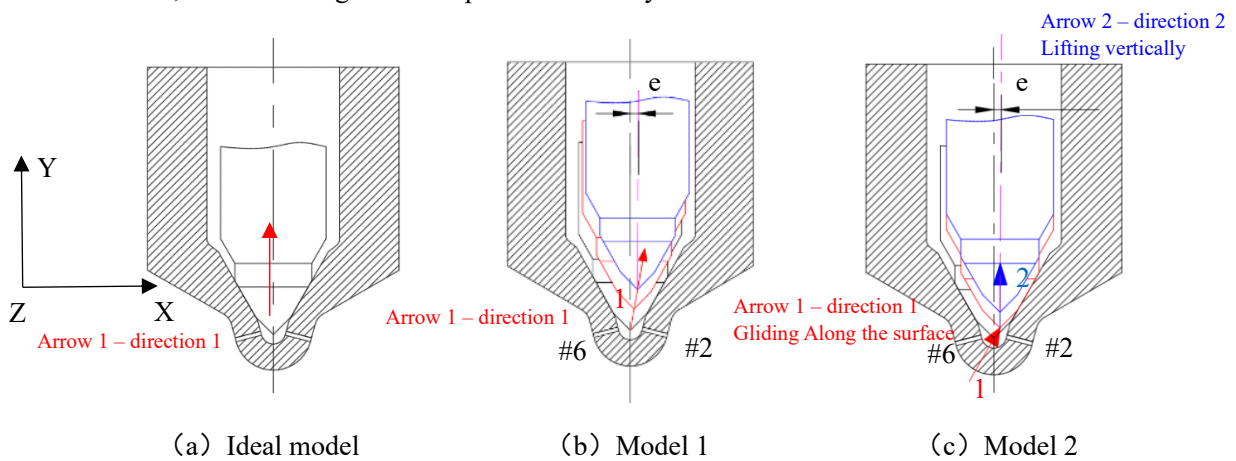
Fig. 4 Mesh sensitivity analysis

224 Fuel properties were set to correspond to the fuel used in experiment as well as the inlet and
225 outlet boundary conditions.

226 2.3 Establishment of the needle eccentric motion

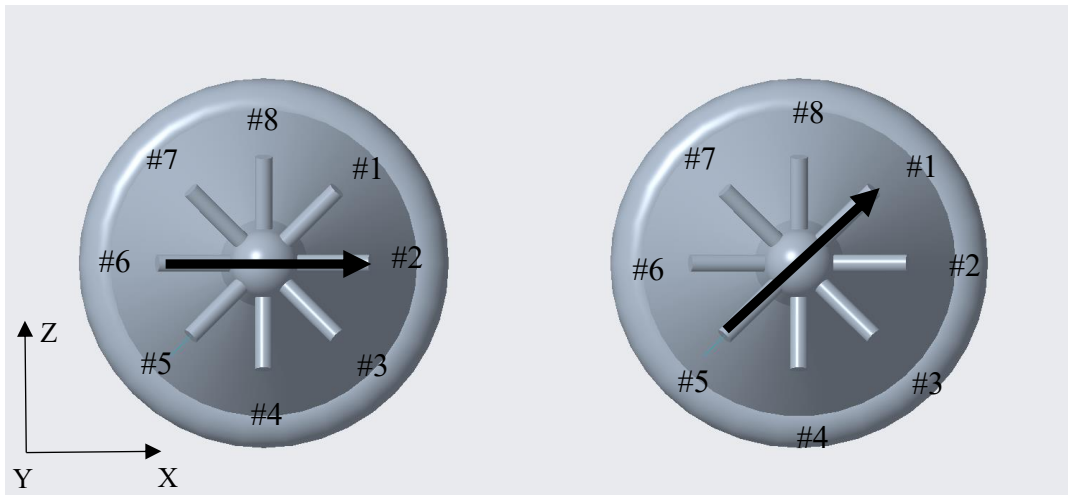
227 Ideally, the nozzle needle lifted vertically upwards along the Y axis, as shown in the Fig. 5(a),
228 which was taken as ideal model. The eccentric motion of the needle is shown in the Fig. 5(b) by the
229 red arrow, which was taken as Model 1. The needle eccentricity is related to the nozzle structure.
230 Although the needle movement in the entire injection process was three-dimensional, the research
231 on the needle eccentric motion considered the lateral and the axial displacement of the needle during
232 the eccentricity in the quest to simplify the computation. The needle reached the largest eccentricity
233 “e” at the maximum lift. The eccentric movement in the figure is located on the X-Y plane, which
234 passes through the centers of the nozzle hole 2 and 6. The needle radially displaces gradually
235 towards hole 2 and away from hole 6 during the eccentric movement.

236 The second eccentric movement model is due to inelastic deformation of the needle (Fig. 5(c)).
 237 At the initial stages the needle displaces under high pressure towards the needle seat. This
 238 displacement results in the radial movement of the needle tip and glides along the needle seat during
 239 the lifting process (needle lift). The needle therefore experiences both radial and axial displacement
 240 during operation. The modelling of this process (needle eccentricity) was conducted in two stages.
 241 As shown in Fig. 5(c), stage 1 (shown by the red arrow 1) is the gliding stage while stage 2 (shown
 242 by the blue arrow 2) is after the gliding stage of the needle. The needle rose along with the needle
 243 seat surface during the stage 1. When the eccentricity reached to the maximum “e” in the radial
 244 direction, the needle began to lift upwards vertically until it reached the maximum lift.



245 Fig. 5 Needle eccentric motion diagram

246 As shown in Fig. 6, two different directions of the needle eccentricities were considered. The
 247 first (0° deflection) involved the radial displacement of the needle tip towards hole 2 (i.e. away from
 248 hole 6) while the second (45° deflection) involved the radial displacement towards hole 1 (i.e. away
 249 from hole 5).



(a) 0° deflection

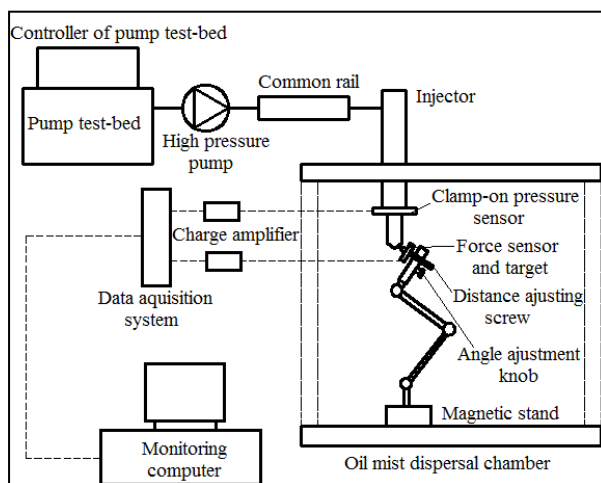
(b) 45° deflection

Fig. 6 Sectional views of injection nozzle at different eccentrical direction

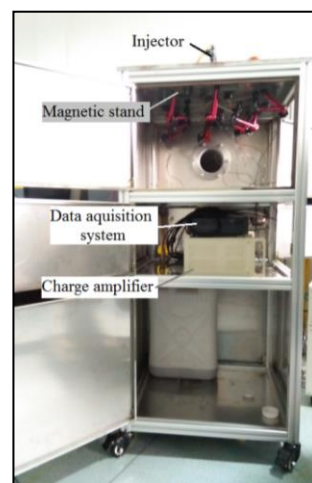
3 Simulation and experimental validation

3.1 Experimental equipment

The schematics of the developed spray momentum flux experimental setup used for model validation is illustrated in Fig. 7 (a). Also in Fig. 7 (b) is the pictorial view of the momentum flux experimental setup.



(a)



(b)

Fig. 7 Diagrammatic illustrations of the experimental setup with all the sections labeled in

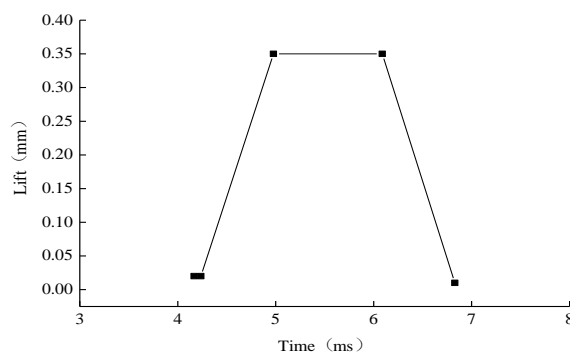
(a) the schematic and (b) the pictorial views respectively

259 It should be noted from Fig. 7 that the electronic control unit (ECU) contained in the high-
260 pressure pump sent signals to the injector solenoid valve to be executed with regards to the operating
261 conditions. A customized magnetic stand equipped with a distance adjusting screw and an angle
262 adjustment knob, allowed the target-sensor assembly to be moved within the required range needed
263 for optimum spray impact. Piezoelectric force sensors placed at required distances from the nozzle
264 hole outlets, converted the force they experienced as a result of the spray impact on them into charge
265 signals. The signals measured were then amplified by a charge amplifier (PPM-12KA-610) and then
266 transmitted to a sixteen-channel data acquisition system (UA326H-16) for analysis. The data was
267 then displayed on a computer monitor and recorded for subsequent processing[36].

268 3.2 Validation of the model

269 In this study, the validation of the model was performed at the following conditions: injection
270 frequency of 6 Hz, injection pulse width of 2000 μ s and rail pressure of 100 MPa.

271 The needle lift profile in Fig. 8 was prescribed and assumed based on experimental injection
272 rate results. To simplify the model and reduce the calculation time, the lift rate at the opening and
273 closing phase were set based on experimental results obtained in other literatures[9,10,40].

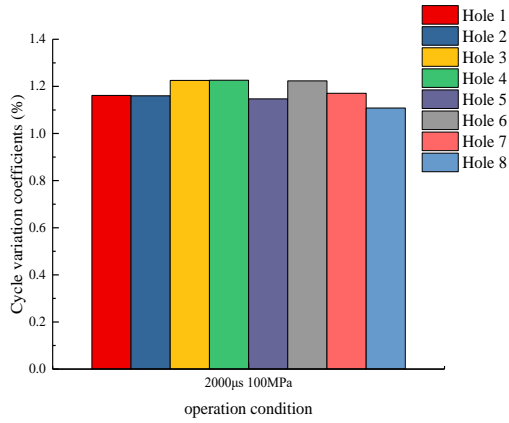


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275

Fig. 8 The one-dimensional needle profile

276 The experimental injection rates were calculated by averaging 100 cycles. The cycle variation
277 for shot-to-shot is under 1.25 % in Fig 9. Hence, ensuring the repeatability of the experiment.



278

279

Fig. 9 Orifice-to-orifice experiment cycle variation coefficients

280

(Injection width pulse 2000 μ s, injection pressure 100 MPa)

281

Fig. 10 and Tab.1 show the nozzle's hole-to-hole experimental injection rate results and the

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simulated injection rate results. It can be seen that the lower layered nozzle hole (1, 3, 5, 7) have

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higher injection rates than the upper layered nozzle holes (2, 4, 6, 8). The simulation results show

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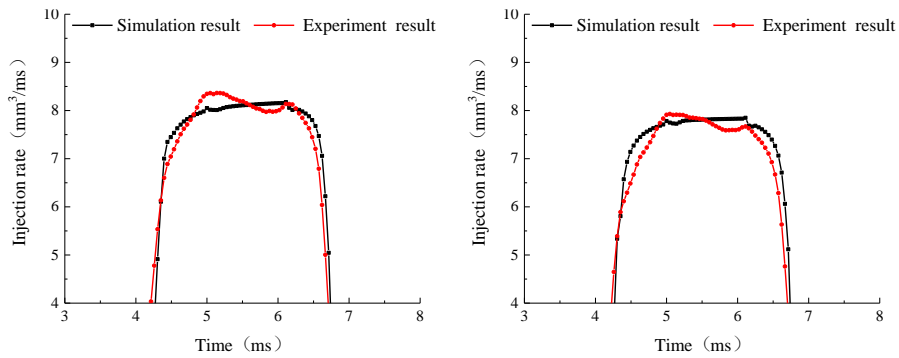
that the two sets of injection rate curves are consistent with each other. They are fully in line with

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the expected results (theoretically). Nonetheless, it is clear from experiment results that the lower

286

layered nozzle holes have higher injection rates than the upper layered nozzle holes

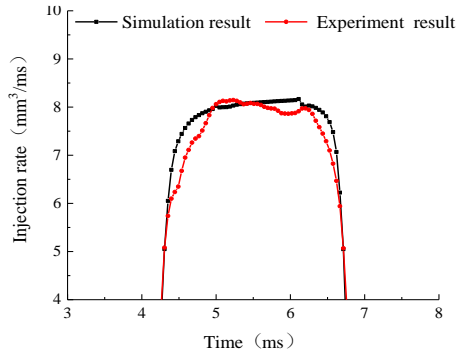


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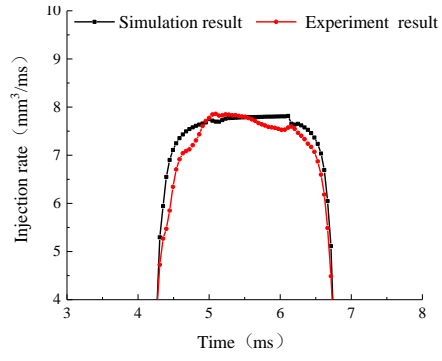
(a) Hole 1

(b) Hole 2

288



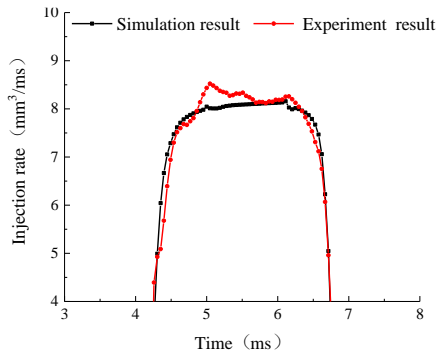
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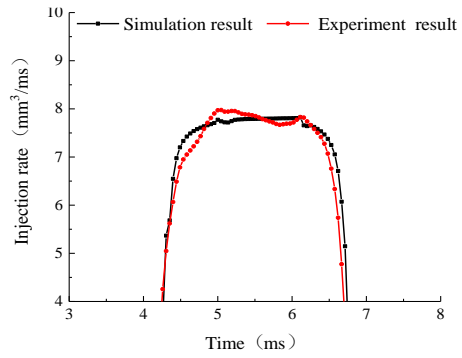
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(c) Hole 3

(d) Hole 4



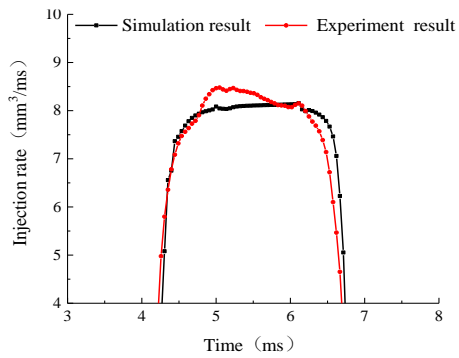
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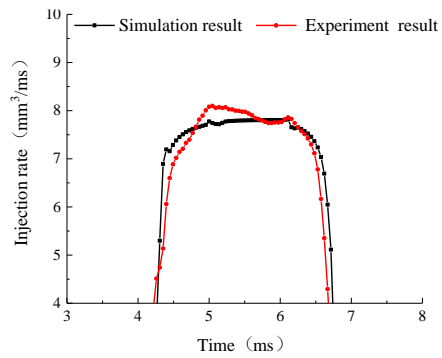
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(e) Hole 5

(f) Hole 6



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(g) Hole 7

(h) Hole 8

295

Fig. 10 Orifice-to-orifice experiment and simulation results of injection rate comparison

296

(Injection width pulse 2000 μ s, injection pressure 100 MPa)

297

Tab. 1 Orifice-to-orifice experiment and simulation results of peak rate of injection comparison

Peak rate of injection (mm^3/ms)							
Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	Hole 8

Simulation	8.24	7.93	8.21	7.84	8.23	7.86	8.23	7.84
Experiment	8.36	7.92	8.14	7.85	8.52	7.98	8.48	8.10

298

Tab. 2 Orifice-to-orifice experiment and simulation results of injection quantity comparison

	Injection quantity (mm ³)							
	Hole 1	Hole 2	Hole 3	Hole 4	Hole 5	Hole 6	Hole 7	Hole 8
Simulation	19.49	18.81	19.29	18.59	19.28	18.65	19.56	18.72
Experiment	19.39	18.65	18.84	18.04	19.46	18.37	19.27	18.44

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The cycle fuel injection quantity computed from simulation ($q_{simulation}$) and the cycle fuel injection quantity computed from experiment ($q_{measure}$) are obtained by integrating the injection rates throughout the injection duration. The relative error between the simulated and experimental result were computed with the expression:

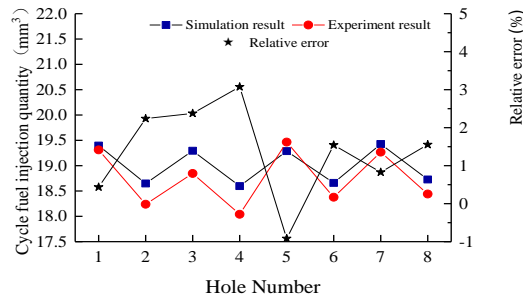
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$$\Delta_{hole} = \frac{q_{simulation} - q_{measure}}{q_{measure}} \times 100\% \quad (8)$$

304

From Fig. 11 and Tab.2, it can be seen that the fuel injection rates and the cycle fuel injection quantities of the lower layered nozzle holes (1,3,5,7) are 4-8 % higher than those of the upper layered nozzle holes (2,4,6,8). The relative error is under 5 %.

306



307

308

Fig. 11 Hole-to-hole experiment and simulation cycle fuel injection quantities

309

(Injection width pulse 2000 μ s, injection pressure 100 MPa)

310 **4 Results analysis and discussion**

311 **4.1 Effect of needle eccentricity on injection characteristics**

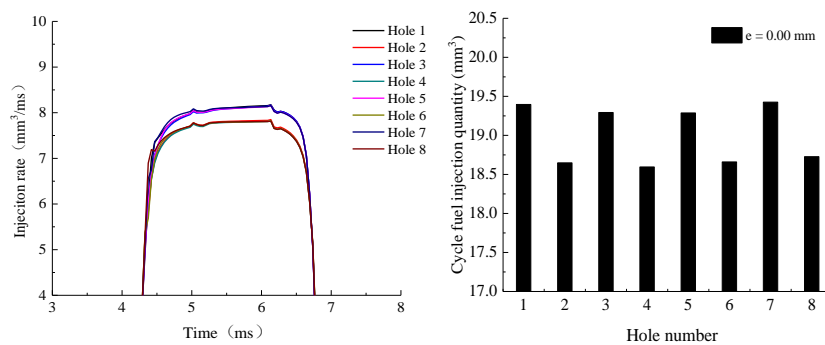
312 The needle valve of high-pressure diesel injectors undergoes lateral movement and
313 deformation, while the continuous increase in injection pressure enlarges the gap of the needle valve
314 assembly. The previous simulation and experiment showed that the range of the needle displacement
315 was from 0.02 mm to 0.065 mm[27,28,41]. Therefore, the radial displacement of the needle
316 eccentricity was set to 0.02 mm 0.04 mm and 0.06 mm for the research.

317 The models will be classified as Ideal model for Fig. 5 (a), Model 1 for Fig. 5 (b) and Model 2
318 for Fig. 5 (c). The upper and lower layers are distributed equally because it is a symmetrical spray
319 injector. The eccentric motion of the needle is radially displaced toward the injection hole 2 and
320 away from the injection hole 6. The nozzle holes “1 and 3”, “5 and 7” and “4 and 8” are symmetric,
321 hence only hole 1, hole 2, hole 4, hole 5 and hole 6 will be discussed next. “+” represents the rising
322 process.

323 In Model 1, the injection rates of injection hole 1 and 2 begin to increase rapidly in the middle
324 of the needle opening stage (+20 % lift~ +57 % lift) (Fig. 12 (b)). The hole 6 records the lowest
325 injection rate. The difference among the injection rates from the same layered holes increases as the
326 needle continuous to lift. In Model 2, the displace needle rises by gliding along surface of the needle
327 seat in the initial stages of needle lift. It causes a narrow flow area around hole 2 and therefore
328 restricts fuel flow through the hole. The injection rate of hole 2 has the slowest development as a
329 result (Fig. 12(c)). The injection rate of hole 1 is not affected so much since the needle radially
330 displaced away from it. When the needle is fully opened, the injection rates of hole 1 and 2 of the
331 two eccentric models are higher than the injection rate of other nozzle holes in the same layer. Hole

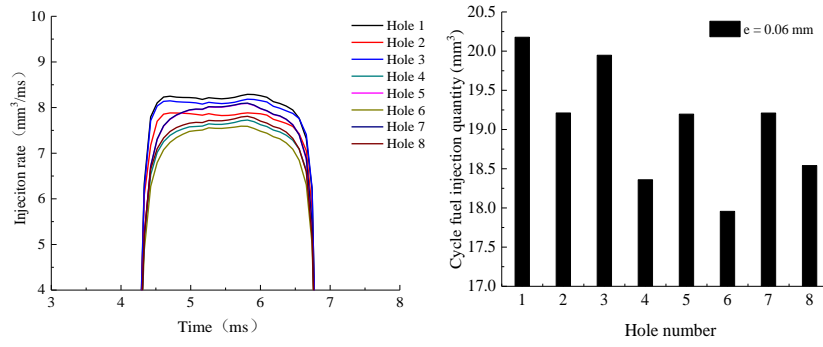
332 6 has the smallest injection rate. The needle eccentricity causes asymmetric flow of fuel. Torelli[42]
 333 achieved the similar tendency.

334 The duration of the gliding movement by the needle on the needle guide, increases with the
 335 increase of the radial displacement of the needle. Therefore, the injection quantity of injection hole
 336 1 and 2 of Model 2 is smaller than the injection quantities from holes 1 and 2 of Model 1. The
 337 injection quantity of hole 6 in Model 1 is the least of all the holes because the injection rate of the
 338 hole 6 is the lowest throughout the whole process. In Model 2, hole 4 has the lowest cycle injection
 339 quantity in the same layer. The needle displaced much closer to hole 4 than hole 6 during the first
 340 opening stage of the needle lift. As shown in Fig. 12 (c), the injection rate of hole 2 and hole 4 is
 341 low. The injection rate of hole 2 increases fast during the second opening stage of the needle and
 342 the injection rate of hole 4 increases slower than the rest of holes. In the fully open stage, the
 343 injection rate of hole 4 is relatively low. The closing process of the needle follows the same trend.
 344 The quantity of fuel flow in the nozzle is depicted by the density of the streamline. That is the denser
 345 the streamline the higher the quantity of fuel flow. Also, the color gives the velocity range of fuel
 346 flow from the bottom view of the nozzle. As shown in the streamline diagram in Fig. 13(c), fuel
 347 flows from hole 4 to hole 1 and also flows from hole 4 and 6 to hole 1 and hole 2 (from the streamline
 348 diagrams). Therefore, the total cycle fuel injection quantity for injection hole 4 is the lowest.



349
 350

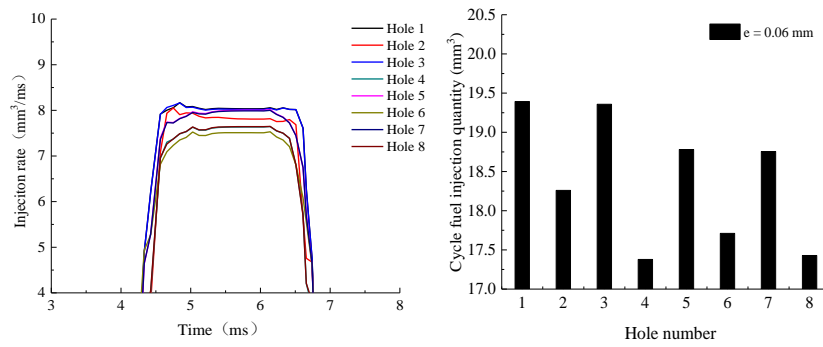
(a) Ideal model



351

352

(b) Model 1



353

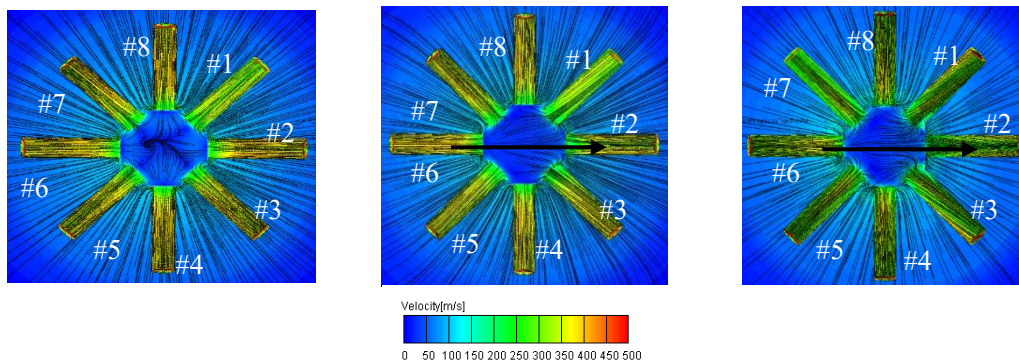
354

(c) Model 2

Fig. 12 Injection rate (left) and cycle injection quantity (right) of

356

each hole with different needle valve motion models at 0.06 mm eccentricity



(a) Ideal model

(b) Model 1

(c) Model 2

357

Fig. 13 Fuel streamlines of different needle motion models when the needle is fully open (bottom view)

358

Integrating the fuel injection rate over the entire injection duration gives the cycle fuel injection

359

quantity of each hole. The relative average deviation is used to describe the difference in the cycle

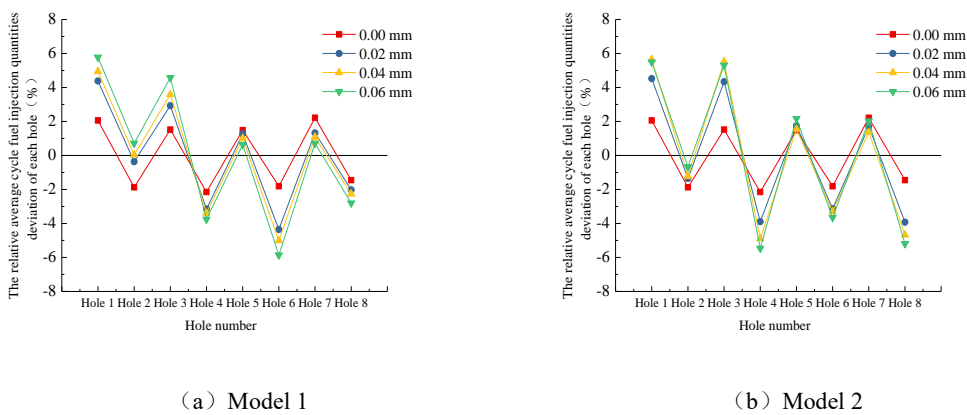
360

fuel injection quantity of each nozzle. The definition is:

361
$$\Delta_1 = \frac{q_i - q_{mean}}{q_{mean}} \times 100\% \quad (9)$$

362 where q_{mean} is the average value (mm^3 / cyc) of the cycle fuel injection quantity in each hole of the
 363 injector; q_i is the cycle fuel injection quantity (mm^3 / cyc) of the hole i ; Δ_1 is the relative average
 364 deviation (%).

365 The two needle eccentricity models have high influences on the uniformity of fuel injection
 366 from the multi hole nozzle as shown in Fig. 14. When the radial displacement of the needle reaches
 367 0.06 mm (during eccentricity) in Model 1, the relative average deviation between the upper layered
 368 holes 2 and 6 is 6.5 % (hole 2,4,6,8 are in the same layer). The difference between the lower layered
 369 holes 1 and 5 is 5 %. The difference between hole 1 and hole 6 (from two different layers) is 11.7 %.
 370 When the radial displacement of the needle reaches 0.06 mm (during eccentricity) in Model 2, the
 371 relative average deviation between the upper layered holes 2 and 6 is 2.7 %. The difference between
 372 the lower layered holes 1 and 5 is 3.3 %. The difference between hole 1 and hole 4 (from two
 373 different layers) is 10.5 %. The degree of non-uniformity increases with increasing needle
 374 eccentricity.



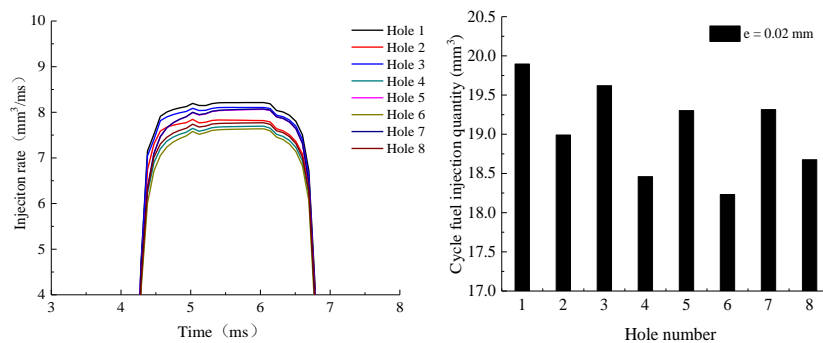
375 Fig. 14 Relative average deviation of hole-to-hole cycle injection quantity

376 at different eccentricities with different needle motion models

377 4.2 Effect of needle eccentric parameters on fuel injection characteristics

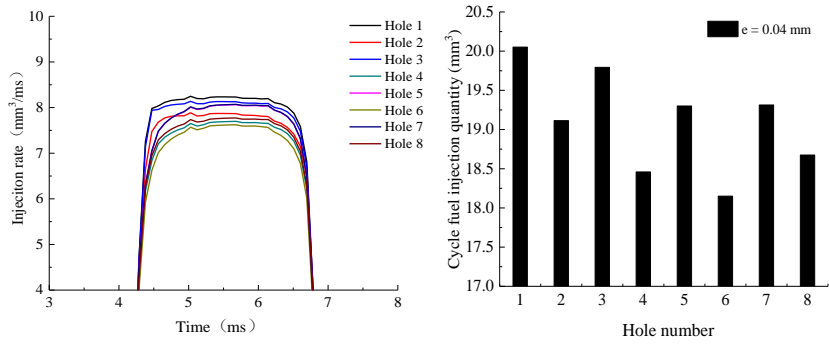
378 The effects of the needle eccentricities and directions of needle displacement on injection
379 characteristics in Model 1 were analyzed. As shown in Fig. 15, the difference in the injection rate
380 of each hole does not change with the increase of the eccentricity in the initial stage of the needle
381 lift. As the needle lifts, the injection rates growth rate of hole 1 and 2 increases rapidly to their
382 maximum values as the eccentricity increases. The growth rate of hole 6 decreases with the increase
383 of the needle eccentricity. Therefore, the fuel injection quantity of the hole 1 and hole 2 increases as
384 the eccentricity increases. The difference in the relative average deviation of the cycle fuel injection
385 quantity of each hole also increases as well.

386 When the needle displaces toward hole 1 (Fig. 15 (d)), the injection rate of nozzle hole 1 attains
387 the highest value comparatively. When the needle is fully opened, there are no significant differences
388 among the remaining holes on the same layer. The relative average deviation differences between
389 the lower layered holes are not apparent (Fig. 16(b)). At eccentricity of 0.06mm, the relative average
390 deviations of the lower layered holes 1 and 5 is 2.7 %. The difference between hole 1 and hole 4
391 (from two different layers) is 9 %. The lower layer holes are not sensitive to needle eccentricity
392 because of their position with regards to the needle displacement.



393 (a) $e=0.02\text{mm}$ (0° deflection)

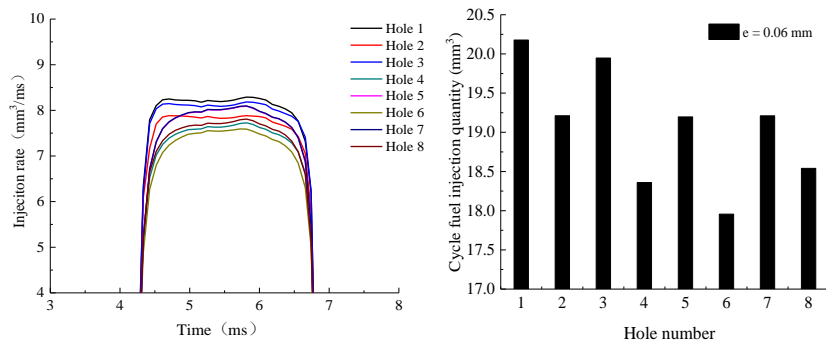
394



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396

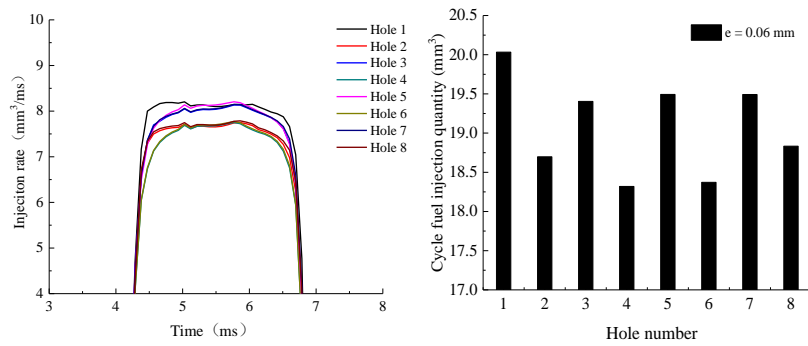
(b) $e=0.04\text{mm}$ (0° deflection)



397

398

(c) $e=0.06\text{mm}$ (0° deflection)



399

400

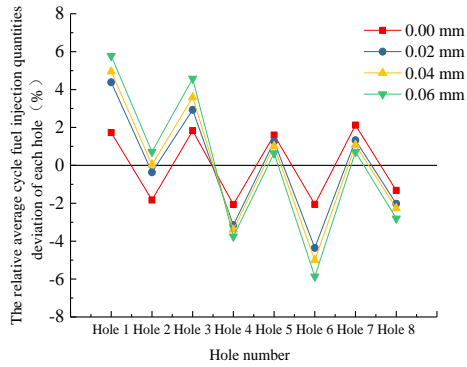
(d) $e=0.06\text{mm}$ (45° deflection)

401

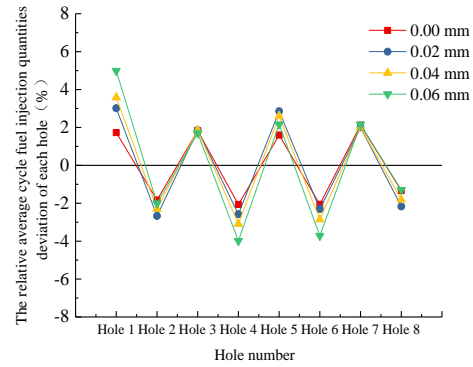
Fig. 15 Injection rate (left) and cycle injection quantity (right) of

402

each hole with different needle eccentric parameters



(a) 0° deflection



(b) 45° deflection

403 Fig. 16 The relative average cycle fuel injection quantities deviation of each hole

404 at different eccentric directions

405 4.3 Effect of needle eccentricity on internal flow characteristics of the nozzle

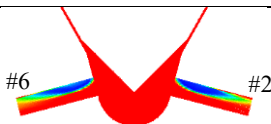
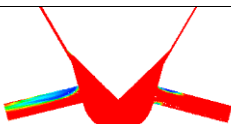
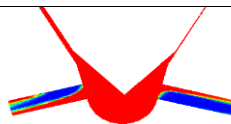


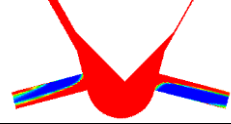

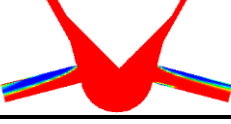
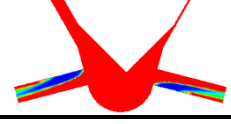
406 The development process and distribution of the cavitation within the holes in the same layer
 407 are similar with each other as in the Ideal model. When the needle moves eccentrically, the
 408 development and distribution of cavitation inside each hole on the upper and lower surfaces of the
 409 holes are quite different.

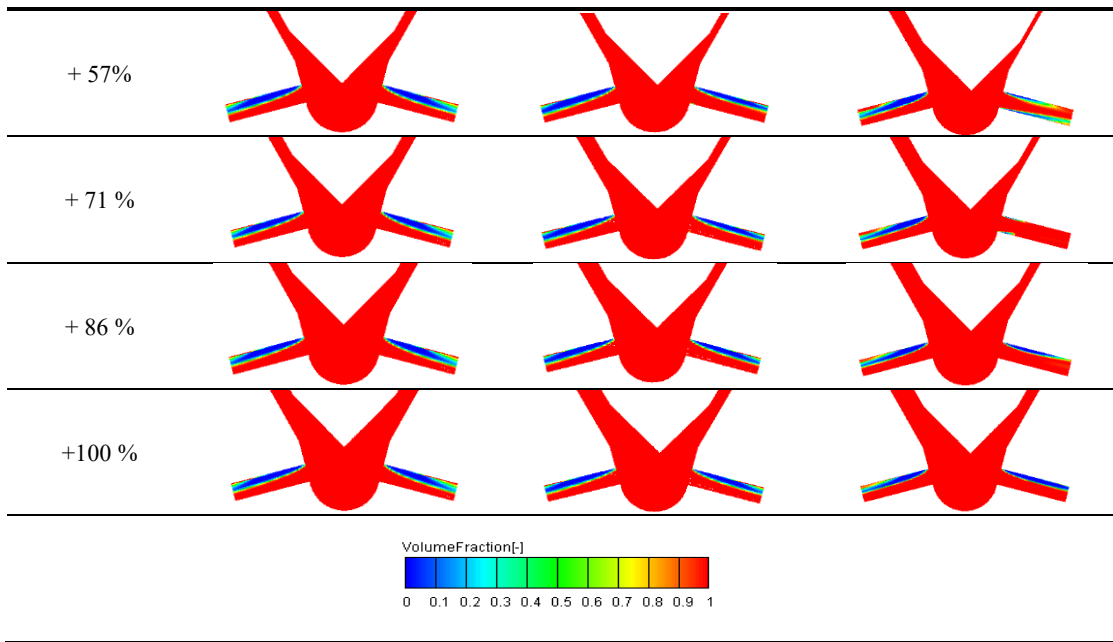
410 Cavitation is characterized by volume fraction. As the gas volume fraction inside the nozzle
 411 hole increases, the cavitation area inside the hole increases. As shown in Tab.3, in Model 1, the
 412 cavitation on the upper surface of hole 2 is small, therefore the primary cavitation is on the lower
 413 surface of hole 2 at +14 % lift. The fuel from the entrance (upper opening) of the injector sac volume
 414 enters the nozzle hole through the bottom while the fuel from the bottom of the injector sac volume
 415 enters the nozzle hole through the top. This is as a result of the geometry of the injector sac volume
 416 and the nozzle holes. Torelli[42] achieved the same tendency. Low pressure areas (that enables the
 417 formation of cavitation) are then created at the top and bottom sections of the nozzle hole (hole 2).
 418 Cavitation is hence formed on both sections of hole 2. The degree of cavitation in the upper surface

419 is stronger than the one formed in the bottom surface at 28% lift. At 43% lift, the cavitation at the
 420 bottom section of the nozzle hole starts to disappear. Nonetheless, the cavitation in hole 2 is weaker
 421 as compared to the cavitation in hole 6. When the needle valve lift is 57 %, the cavitation on the
 422 upper surface of hole 2 tend to be stable and the cavitation on the bottom surface almost disappear,
 423 leaving only a small part. When the needle valve lift is 71%, the cavitation of hole 2 is stable, which
 424 is similar to hole 2 without eccentric movement.

425 The needle glides along the needle body from +14 %~+28 % lift in Model 2. The extremely
 426 narrow flow area in the displaced space causes irregular fuel flow, which results in the formation of
 427 cavitation at the bottom surfaces of hole 2. As the needle lifts vertically, the position of the cavitation
 428 gradually changes from the lower surface to the upper surface of hole 2 with the gradual increase of
 429 the flow area in the displaced space. From +14% to +28% lift, the cavitation formation at the bottom
 430 surface is higher. At +43% lift, the cavitation of hole 2 reduces to half the cavitation at +14% lift.
 431 At +57 % lift, weak cavitation formations appear on the upper and bottom sections of hole 2. At
 432 +71 % lift, the cavitation in nozzle hole 2 almost disappear, leaving tiny cavitation formations on
 433 both upper and bottom surfaces.

434 Tab.3 The cavitation distribution inside holes with different needle motion models (e=0.06mm)

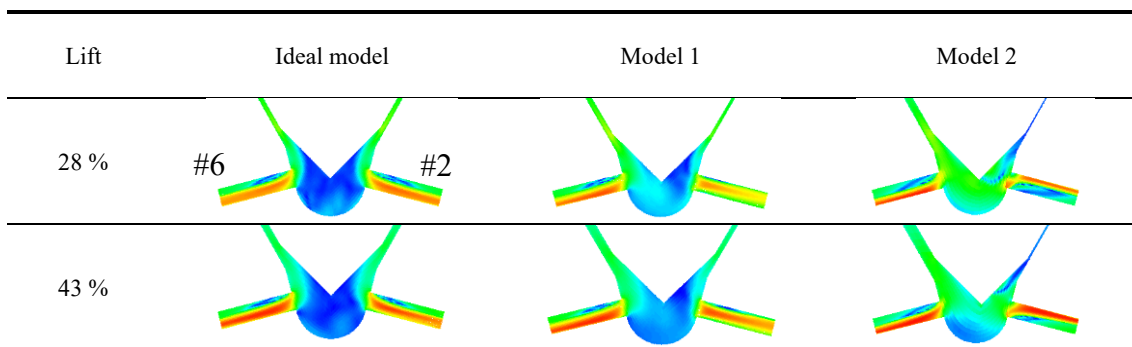
Lift	Ideal model	Model 1	Model 2
+14 %			
+28 %			
+ 43%			

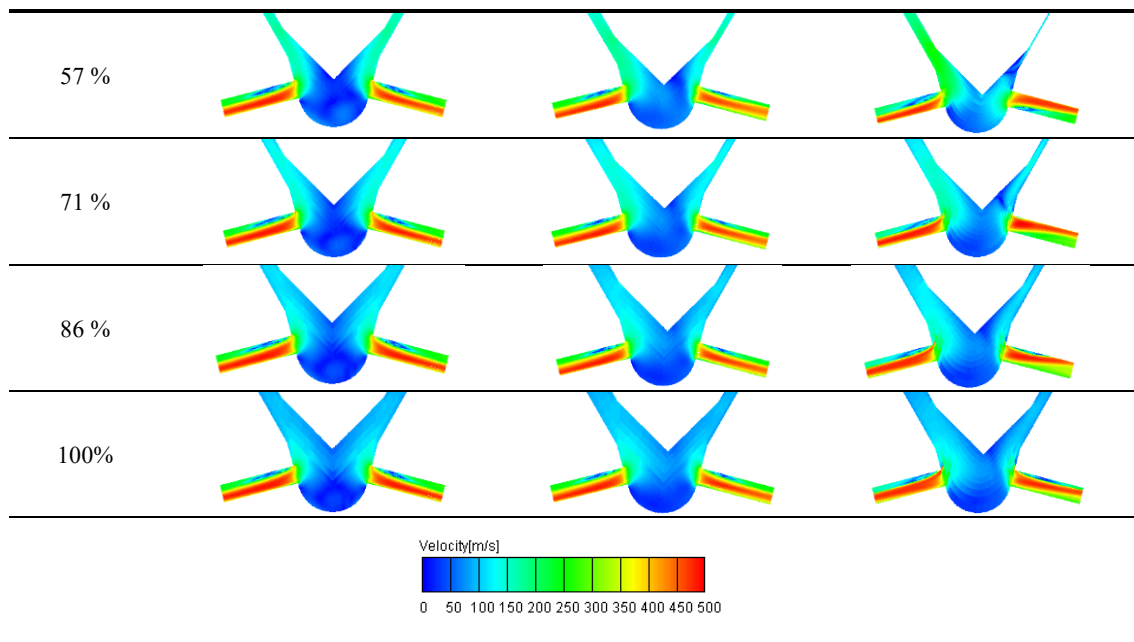


435 As shown in Tab.4, the fuel flow velocity inside hole 2 is higher than the upper and lower
 436 surface of hole 2 in Model 1 due to the cavitation formation at the upper and lower surfaces at 28 %
 437 needle lift. The flow velocity within each nozzle hole during full needle lift is more uniform as
 438 compared to the flow velocities at the initial stages of needle lift in Model 1.

439 In Model 2, high-velocity region in hole 2 is less at + 28 % due to the irregular flow at the
 440 initial stage of the needle lift. The fuel flows into the upper side of hole 2 because of the guiding
 441 effect of the sac and the hole structure. The high- velocity region inside the hole 2 gradually transfers
 442 from the upper surface to the lower surface with the increment of the displaced flow area due to the
 443 changing effect of cavitation at those areas.

444 Tab. 4 The velocity distribution inside holes with different needle motion models ($e=0.06\text{mm}$) .





445 5 Conclusion

446 A three-dimensional (3-D) model of a nozzle which was validated with experimental results
 447 was used to analyze the injection characteristics of each hole. Two different needle eccentricity
 448 models based on inelastic deformation of the needle were established to analyze the effect on the
 449 fuel injection characteristics and internal flow characteristics of each nozzle hole. The first method
 450 only considered the lateral displacement of the needle during needle lift. The needle reached the
 451 largest eccentricity at the maximum lift. The second method took the needle inelastic deformation
 452 into consideration. That is, the needle radially displaces and glides along with the needle seat surface
 453 during needle lift. At maximum radial displacement, the needle lifts vertically upward from the
 454 displaced position. From the result the following were observed:

- 455 1. Each eccentricity models led to asymmetric fuel flow. The transient injection rate
 456 differences between the nozzle holes hole becomes more apparent as the eccentricity
 457 increases. In Model 1, the injection rate of hole 2 (The nozzle hole closest to the needle
 458 displacement) rises rapidly during the opening process. In Model 2, the injection rate of
 459 hole 2 in the initial stages of the needle lift is lower than the injection rates from the other

460 nozzle holes in the same layer. At full needle lift, the fuel injection rate of hole 2 is higher
461 than those from the other injection holes in the same layer.

462 2. The cycle fuel injection quantity of hole 2 increases as the eccentricity of the needle
463 increases in Model 1. The cycle fuel injection quantity of hole 6 (the nozzle hole farthest
464 from the needle displacement) decreases as the eccentricity of the needle increases.
465 Resulting in increasing non-uniformity in fuel injection. The upper layer holes are highly
466 affected by the needle eccentricity, comparatively.

467 3. The cavitation distribution within the nozzle holes in the two needle eccentricity models
468 are quite different. In the first eccentric model, the cavitation intensity of hole 2 is weaker
469 than the one formed in hole 6. The difference gradually disappears when the needle is fully
470 opened. In the second eccentricity model, the cavitation of hole 2 first appears on the lower
471 side at the initial stages and gradually shifts to the upper side as the lifting progresses.

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474 51476072)

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